

Using Denoisers for Accelerated CMR

Plug-and-play methods for supervised and self-supervised recovery

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Conflict

- No conflict to declare

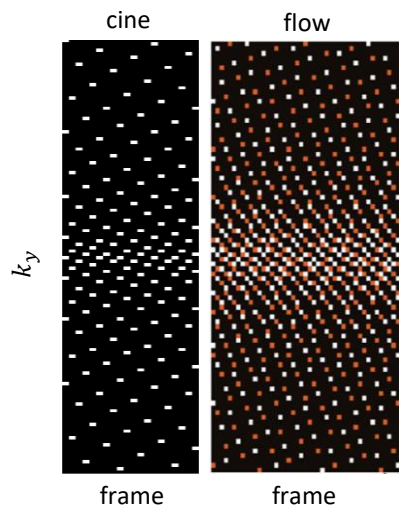


Outline

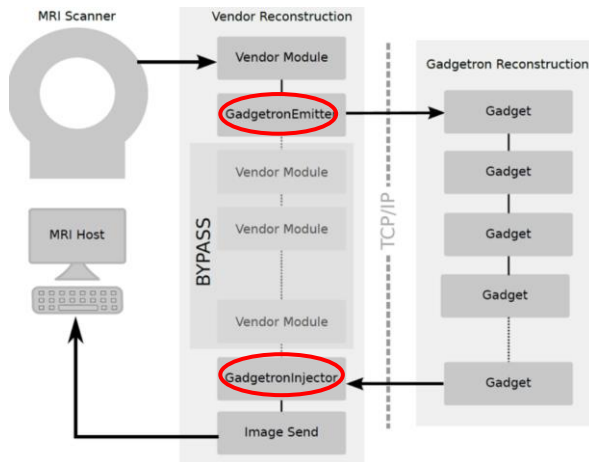
- Plug-and-play (PnP) methods for CMR
- Self-calibrated PnP (ReSiDe)
- Summary

Compressed sensing (CS)

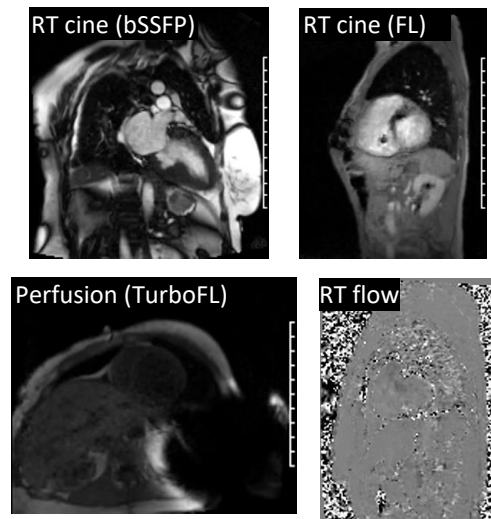
A pseudo-random Cartesian sampling [1,2]



B Gadgetron-based inline reconstruction [3]



C example images from patients

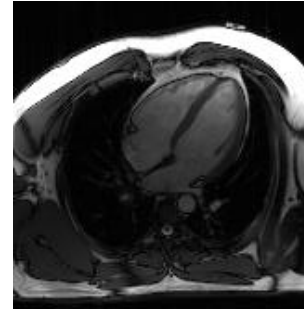
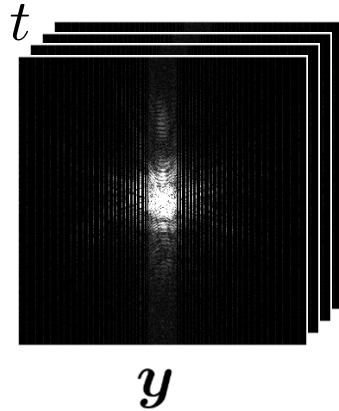


CMR reconstruction beyond CS [1]

- **Blind CS**
 - Lingala and Jacob, IEEE TMI, 2013
- **Low-rank approaches**
 - Zhao and Liang, IEEE TMI, 2012
 - Liu and Sun et al., MRI, 2019
- **Low-rank and sparse approaches**
 - Otazo and Sodickson et al., MRM, 2014
 - Miao and Nayak et al., MRI, 2016
- **Deep learning**
 - Küstner and Prieto et al., Scientific Reports, 2020
 - Hamilton and Seiberlich et al., MRM, 2021

Plug-and-play (PnP) methods

$$\hat{\boldsymbol{x}} = \arg \min_{\boldsymbol{x}} \left\{ \frac{1}{2\tau^2} \|\mathbf{A}\boldsymbol{x} - \boldsymbol{y}\|_2^2 + \phi(\boldsymbol{x}) \right\}$$



From CS to PnP

$$\hat{\mathbf{x}} = \arg \min_{\mathbf{x}} \left\{ \frac{1}{2\tau^2} \|\mathbf{Ax} - \mathbf{y}\|_2^2 + \phi(\mathbf{x}) \right\}$$

Algorithm 1 Primal-dual splitting

Require: $\nu > 0, \tau, \mathbf{A}, \mathbf{y}$

- 1: $\gamma = \frac{\nu}{\tau^2} \|\mathbf{A}\|_2^2, \mathbf{x}_0 = \mathbf{A}^H \mathbf{y}, \mathbf{z}_0 = \mathbf{Ax}_0 - \mathbf{y}$
- 2: **for** $t = 1, 2, 3, \dots$ **do**
- 3: $\mathbf{u}_t = \mathbf{x}_{t-1} - \frac{\nu}{\tau^2} \mathbf{A}^H \mathbf{z}_{t-1}$
- 4: $\mathbf{x}_t = \arg \min_{\mathbf{x}} \left\{ \phi(\mathbf{x}) + \frac{1}{2\nu} \|\mathbf{x} - \mathbf{u}_t\|_2^2 \right\}$
- 5: $\mathbf{v}_t = 2\mathbf{x}_t - \mathbf{x}_{t-1}$
- 6: $\mathbf{z}_t = \frac{\gamma}{1+\gamma} \mathbf{z}_{t-1} + \frac{1}{1+\gamma} (\mathbf{Av}_t - \mathbf{y})$
- 7: **end for**
- 8: **return** $\hat{\mathbf{x}} \leftarrow \mathbf{x}_t$

Line 4 interpretation: denoising of \mathbf{u}_t

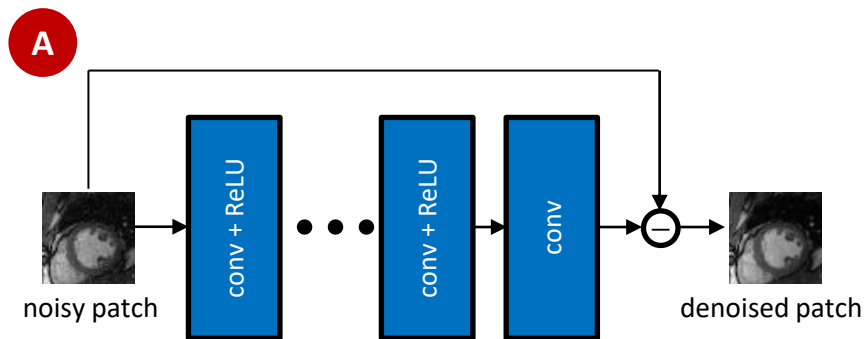
Algorithm 2 PnP Primal-dual splitting

Require: $\nu > 0, \tau, \mathbf{A}, \mathbf{y}, \mathbf{f}$

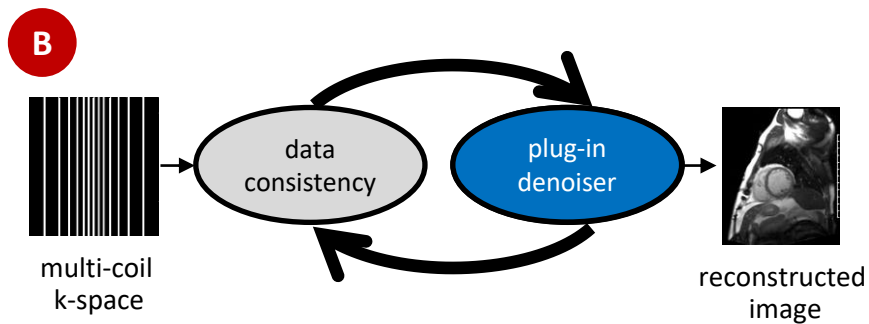
- 1: $\gamma = \frac{\nu}{\tau^2} \|\mathbf{A}\|_2^2, \mathbf{x}_0 = \mathbf{A}^H \mathbf{y}, \mathbf{z}_0 = \mathbf{Ax}_0 - \mathbf{y}$
- 2: **for** $t = 1, 2, 3, \dots$ **do**
- 3: $\mathbf{u}_t = \mathbf{x}_{t-1} - \frac{\nu}{\tau^2} \mathbf{A}^H \mathbf{z}_{t-1}$
- 4: $\mathbf{x}_t = \mathbf{f}(\mathbf{u}_t)$
- 5: $\mathbf{v}_t = 2\mathbf{x}_t - \mathbf{x}_{t-1}$
- 6: $\mathbf{z}_t = \frac{\gamma}{1+\gamma} \mathbf{z}_{t-1} + \frac{1}{1+\gamma} (\mathbf{Av}_t - \mathbf{y})$
- 7: **end for**
- 8: **return** $\hat{\mathbf{x}} \leftarrow \mathbf{x}_t$

$\mathbf{f}(\cdot)$: apply any denoiser

PnP with application-specific denoisers



an application-specific, learned denoiser can benefit PnP [1,2]



PnP methods “plug in” a denoiser into the reconstruction [3]

Training independent of the forward model

✓ Highly generalizable

Physics-driven modeling

✓ State-of-the-art performance

Training on image patches

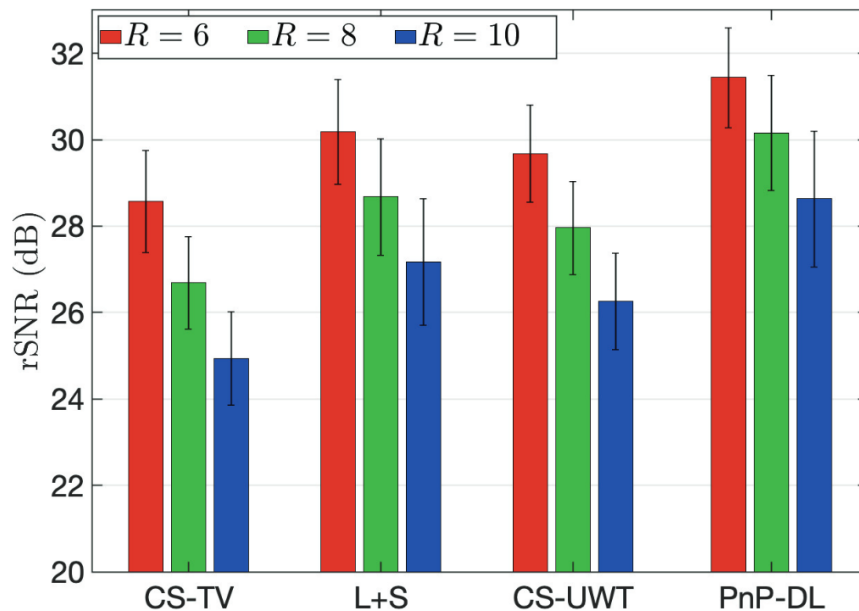
✓ Access to fully sampled k-space data not required

Iterative reconstruction

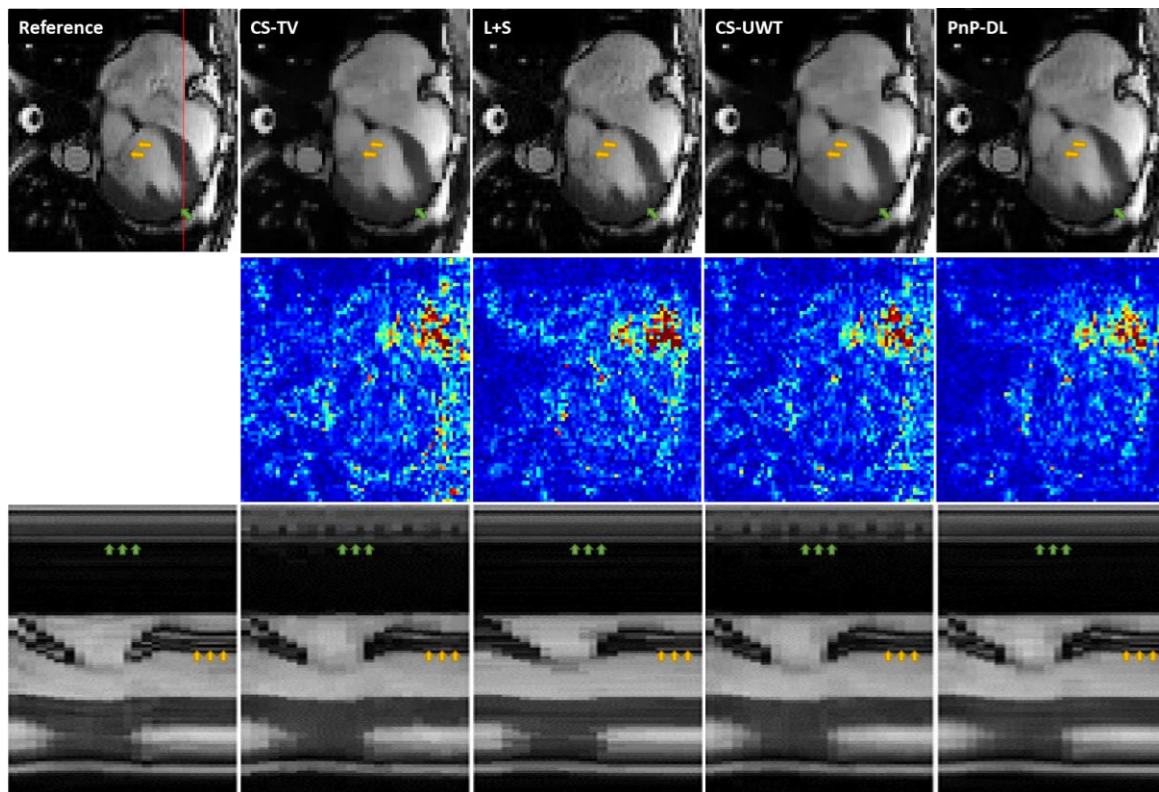
✗ Slower than some other deep learning methods

PnP for segmented 2D cine

- **Training:** DL denoiser trained on 50 fully-sampled, breath-held cine images
- **Validation:** Nine retrospectively undersampled datasets at $R = 6, 8,$ and 10



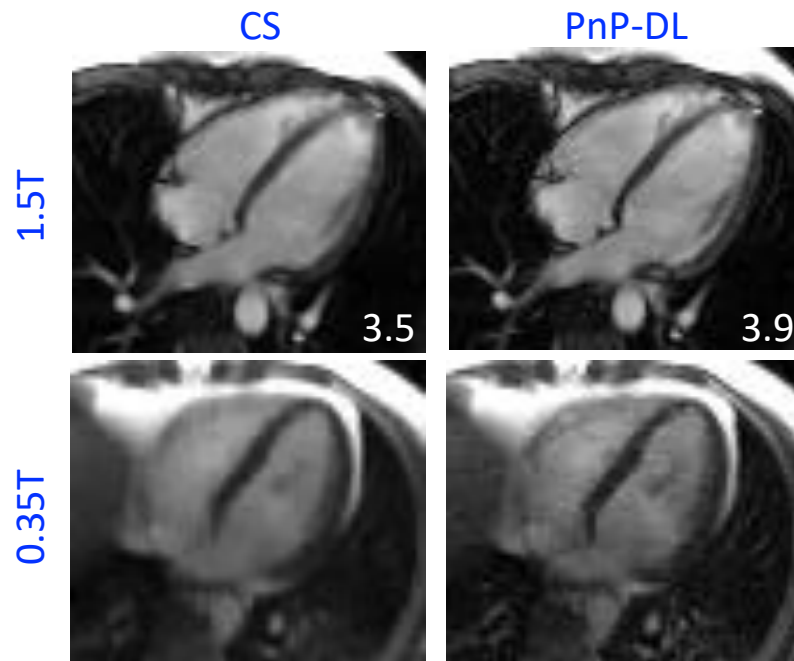
PnP for segmented 2D cine



validation for the axial slice—the view not included in the training

PnP for real-time 2D cine

- **Training:** DL denoiser trained on 50 fully sampled, breath-held cine images
- **Validation:** Ten **prospectively** undersampled real-time datasets scored by an expert (1—5)



ReSiDe: Recovery with a self-calibrated denoiser

Algorithm 2 PnP Primal-dual splitting

Require: $\nu > 0, \tau, \mathbf{A}, \mathbf{y}, f$

- 1: $\gamma = \frac{\nu}{\tau^2} \|\mathbf{A}\|_2^2, \mathbf{x}_0 = \mathbf{A}^H \mathbf{y}, \mathbf{z}_0 = \mathbf{A} \mathbf{x}_0 - \mathbf{y}$
- 2: **for** $t = 1, 2, 3, \dots$ **do**
- 3: $\mathbf{u}_t = \mathbf{x}_{t-1} - \frac{\nu}{\tau^2} \mathbf{A}^H \mathbf{z}_{t-1}$
- 4: $\mathbf{x}_t = f(\mathbf{u}_t)$
- 5: $\mathbf{v}_t = 2\mathbf{x}_t - \mathbf{x}_{t-1}$
- 6: $\mathbf{z}_t = \frac{\gamma}{1+\gamma} \mathbf{z}_{t-1} + \frac{1}{1+\gamma} (\mathbf{A} \mathbf{v}_t - \mathbf{y})$
- 7: **end for**
- 8: **return** $\hat{\mathbf{x}} \leftarrow \mathbf{x}_t$

$f(\cdot)$: apply any denoiser

Algorithm 3 ReSiDe

Require: $\nu > 0, \tau, \mathbf{A}, \mathbf{y}, f$

- 1: $\gamma = \frac{\nu}{\tau^2} \|\mathbf{A}\|_2^2, \mathbf{x}_0 = \mathbf{A}^H \mathbf{y}, \mathbf{z}_0 = \mathbf{A} \mathbf{x}_0 - \mathbf{y}$
- 2: **for** $t = 1, 2, 3, \dots$ **do**
- 3: $\tilde{\mathbf{x}}_{t-1} = \mathbf{x}_{t-1} + \mathcal{N}(\mathbf{0}, \sigma_t^2 \mathbf{I})$
- 4: $\boldsymbol{\theta}_t = \operatorname{argmin}_{\boldsymbol{\theta}} \sum_{i=1}^P \mathcal{L}(f(\mathcal{I}[\tilde{\mathbf{x}}_{t-1}]_i; \boldsymbol{\theta}), \mathcal{I}[\mathbf{x}_{t-1}]_i)$
- 5: $\mathbf{u}_t = \mathbf{x}_{t-1} - \frac{\nu}{\tau^2} \mathbf{A}^H \mathbf{z}_{t-1}$
- 6: $\mathbf{x}_t = f(\mathbf{u}_t; \boldsymbol{\theta}_t)$
- 7: $\mathbf{v}_t = 2\mathbf{x}_t - \mathbf{x}_{t-1}$
- 8: $\mathbf{z}_t = \frac{\gamma}{1+\gamma} \mathbf{z}_{t-1} + \frac{1}{1+\gamma} (\mathbf{A} \mathbf{v}_t - \mathbf{y})$
- 9: **end for**
- 10: **return** $\hat{\mathbf{x}} \leftarrow \mathbf{x}_t$

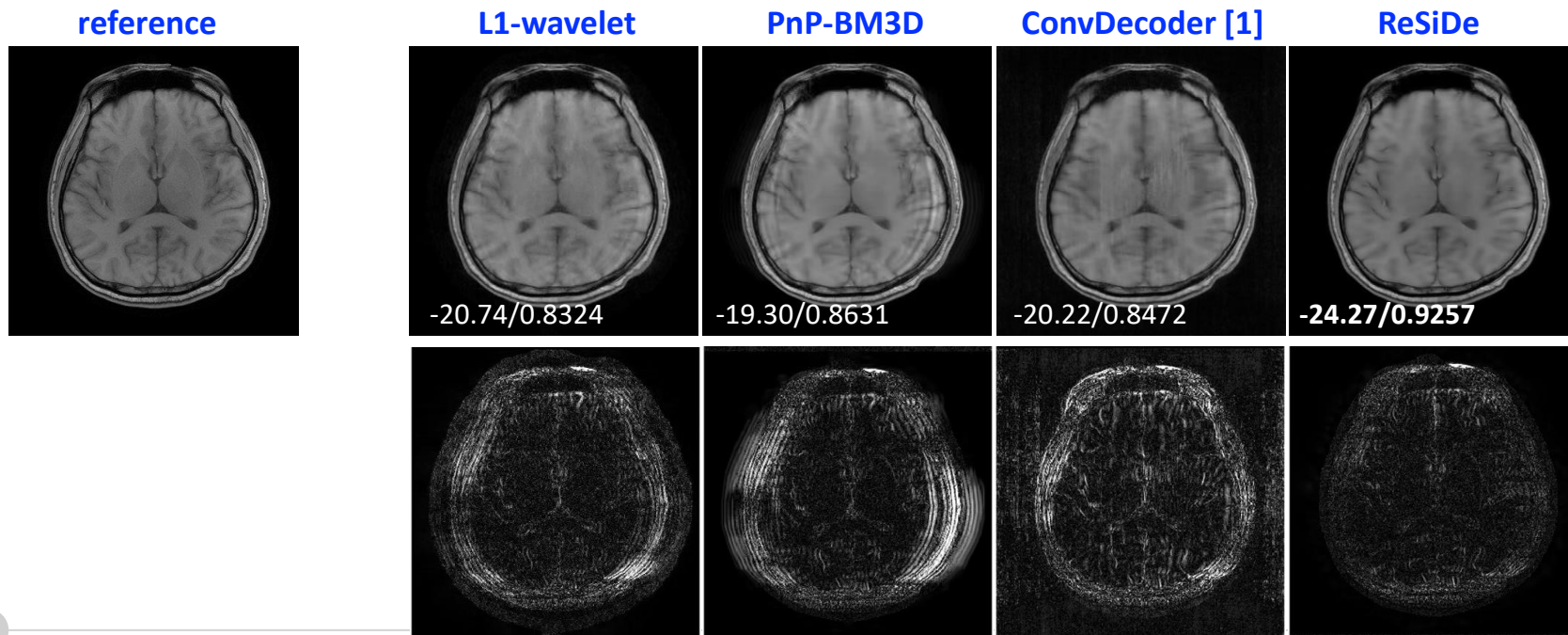
Line 3: Add noise to \mathbf{x}_{t-1}

Line 4: Train a denoiser to remove the added noise

$f(\cdot; \boldsymbol{\theta}_t)$: apply the self-calibrated denoiser

ReSiDe—brain imaging

- **Data:** Multi-coil T1/T2-weighted images from fastMRI.org
- **Sampling:** R=2 and 4, random + ACS, pseudo-random + ACS



ReSiDe—brain imaging

T1	R=2, pseudo-random	R=4, pseudo-random	R=2, random	R=4, random
L1-wavelet	-27.44 / 0.8973	-24.71 / 0.8707	-26.59 / 0.8892	-20.74 / 0.8324
PnP-BM3D	-28.60 / 0.9610	-25.29 / 0.9361	-27.22 / 0.9494	-19.30 / 0.8631
ConvDecoder	-25.74 / 0.9324	-22.89 / 0.9051	-25.82 / 0.9391	-20.22 / 0.8472
ReSiDe	-28.62 / 0.9580	-25.97 / 0.9318	-28.06 / 0.9491	-24.27 / 0.9257

T2	R=2, pseudo-random	R=4, pseudo-random	R=2, random	R=4, random
L1-wavelet	-29.52 / 0.9683	-23.83 / 0.9375	-26.78 / 0.9558	-22.09 / 0.9286
PnP-BM3D	-28.73 / 0.9573	-24.22 / 0.9414	-27.24 / 0.9548	-23.40 / 0.9370
ConvDecoder	-24.44 / 0.9401	-20.21 / 0.9014	-24.22 / 0.9370	-19.76 / 0.8987
ReSiDe	-30.05 / 0.9684	-25.18 / 0.9404	-28.35 / 0.9654	-24.55 / 0.9402

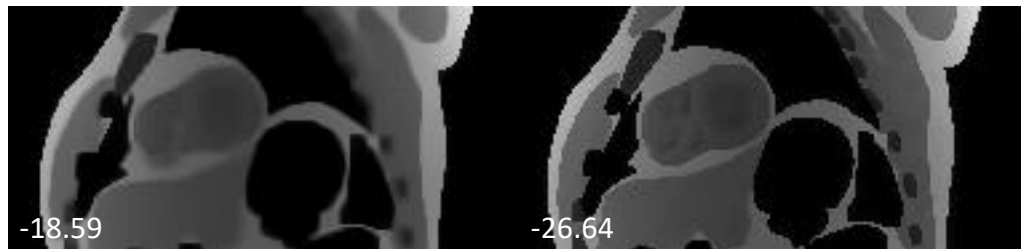
ReSiDe—dynamic phantom

- **Data:** Multi-coil MRXCAT digital phantom [1]
- **Sampling:** Pseudo-random Cartesian, R=8

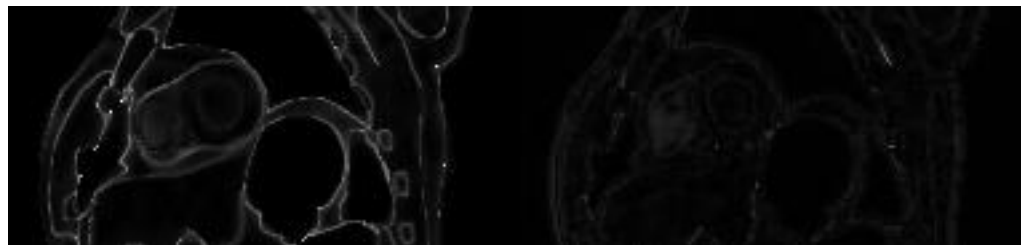
reference



PnP-BM4D



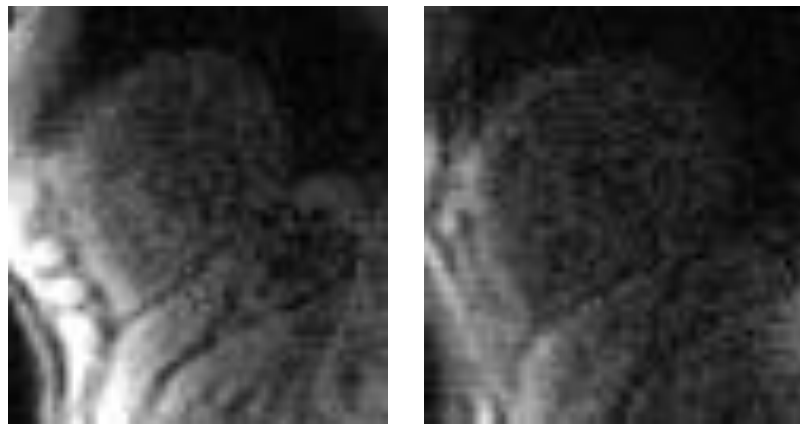
ReSiDe



ReSiDe—perfusion imaging

- **Data:** A clinical first-pass perfusion at 1.5T
- **Sampling:** Rate-2 EPI

GRAPPA



ReSiDe



Connection of other self-calibrated methods

- **There is growing literature on training denoisers from imperfect images.**
 - Noise2Noise
 - *Lehtinen and Aila et al., arXiv, 2018*
 - Noise2Self
 - *Batson and Royer, MLR, 2019*
 - Noise2Void
 - *Krull and Jug et al., CVF, 2019*
 - Noisy-as-clean
 - *Xu and Shao et al., IEEE TIP, 2020*
 - Unsupervised learning with SURE
 - *Zhussip and Chun et al., NeurIPS, 2019*
 - *Metzler and Baraniuk et al., arXiv, 2020*
 - *Aggarwal and Jacob et al., ICASSP, 2021*

Summary

- PnP methods can leverage the power of DL by employing application-specific learned denoisers
- Many of the existing algorithms developed for CS can be used for PnP
- The denoiser can be trained on image patches
- By training the denoiser from the image that is being recovered, PnP can facilitate self-calibrated imaging

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